



Proof of Work and Blockchains

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Proof of Work



- Challenger provides puzzle
- Solver expends resources to solve puzzle

Proof of Work

A variety of uses [Jakobbson+Juels'99]

- Spam protection [Dwork+Naor'92]
- construction of digital time capsules
 [Goldschlag+Stubblebine'89, Rivest+'96]
- Server access metering [Franklin+Malkhi'97]
- (D)DoS protection [Juels+Brainard'99]
- Digital money minting [Rivest+Shamir'01]
- Sybil protection [Apsnes'15]

... but botnets?

How Hard?



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PoW for Blockchains

- Bitcoin [Nakamoto'08]: PoW for Sybil protection, With a trick: direct monetary compensation
- The result: Wildly successful and incredibly robust But also:

some surprising properties

A Replicated State Machine



The Blockchain



PoW for Blockchains

- Log in blocks
- Solve puzzle to add block
- Get prize per block
- On a fork (a natural event), stronger side wins



Basic Operation

• Puzzle is a function of current and previous block. (e.g., their hash smaller than target)



- Real-world participation cost
- Burn real-world resources, committing to a state machine history

PoW in a Blockchain

- Block every set interval (10min, 15sec)
- Automatically adjusting difficulty ==> a lottery of sorts ==> bustling mining industry

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Bitcoin

prize decay ==> FOMO at work Also finite supply, deflation

Waste?

- Real-world waste
 - Compute power (sha256 ^2) Really power (Watts)
 - Less useless (Primecoin)
 - Storage [Miller+'14]
 - Hardware (PoET)
- No real-world waste
 - Permissioned (Hyperledger, Stellar), or
 - Pending formal discussion (Proof of Stake)

Resilience

- Surprisingly stable
 - Strategic mining (Selfish mining etc. not seen in the wild)
- Few blockchain alternatives
 - GHOST +variants (Ethereum, DECOR) [Sompolinsky+Zohar'15, Lewenberg+'15]
 - Bitcoin-NG +variants (Hybrid consensus, Byzcoin)

Pooled Mining

Blockchain Mining



Constant rate : globally updated Difficulty

Pooled Mining

Many miners Constant PoW rate



Miners form **pools**



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Open Pools and Centralization

- Miners form pools
- Largest are open pools
- Lead to centralization





A threat to the blockchain's basic premise

Pool Block Withholding Oakland'15





Attacker:

- Registers as standard miner
- Uses some miners as moles



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Factors influencing revenue



Less miners ==> reduced difficulty

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The Pool Game

Goal Maximize *revenue density*

Round One pool updates infiltration rates

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Analysis

- Stable state (equilibrium)
- Generic (any pool size)





Analysis

One Attacker



Game progress:

One round – attacker optimizes $r_1(x_{1,2})$

Dominant strategy: Attack

Honest pool mining is not an equilibrium



In general: Honest pool mining is not an equilibrium

(For any two pools, one should attack)

Two Attackers



Game progress

Repeatedly:

- 1. Pool 1 optimizes $r_1(x_{1,2}, x_{2,1})$
- 2. Pool 2 optimizes $r_2(x_{2,1}, x_{1,2})$

A single feasible equilibrium point

When both pools are minorities of any size: **pool 1**

		NO ATTACK	ATTACK
pool 2	NO ATTACK		
	ATTACK		

When both pools are minorities of any size: **pool 1**



One Attacker



When both pools are minorities of any size: **pool 1**



When both pools are minorities of any size: **pool 1**



Two Attackers



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When both pools are minorities of any size: **pool 1**



When both pools are minorities of any size: **pool 1**



This is good

When both pools are minorities of any size: **pool 1**



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Iterated game with unbounded rounds ==> Possible non-equilibrium stable state

Detection
 Does not work



- Detection
 Does not work
- Bonus for full PoW / seniority
 Reduces revenue homogeneity





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- Honey pot
 Wastes resources



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- Out of band enforcement
 Implies small trust circles



System Health



Conclusion

- Proof of work: cornerstone of open blockchains
 - Some waste
 - Effective security (being proven in retrospect)
- Architecture leads to surprising properties
 - The miner's dilemma
 - Pooled mining
 - Industrial mining
 - Selfish mining

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- Non-standard proof-of-work
- Proof of work outsourcing
- Proof of work in face of chain forks